## From $\bar{K}$ bound states to $\bar{K}$ condensation? Avraham Gal

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Based on D. Gazda, E. Friedman, A. Gal, J. Mareš :  $\bar{K}$  and multi- $\bar{K}$  nuclei, PRC **76**, 055204 (2007) Multi- $\bar{K}$  nuclei and kaon condensation, arXiv:0801.3335

no accepted \$\overline{K}\$ bound states at present (KEK, Frascati)
chance for narrow states with \$B\_{\overline{K}}\$ ~ 100 - 200 MeV?
is \$\overline{K}\$ condensation limiting case of \$\overline{K}\$ bound states?
\$\overline{K}\$ cond on Earth (lab) or in Heaven (neutron stars)?



W. Weise, R. Hartle, arXiv:0801.1467, NPA (in press) Forward  $F_{K^-p}$  in SU(3) chiral  $\overline{K}N - \pi Y$  model from BNW, EPJA 25 (2005) 79  $\rightarrow V_{\overline{K}}(\rho_0) \sim -100$  MeV



J. Schaffner-Bielich, NPA (in press) updated arXiv:astro-ph/0703113 Neutron-star composition with density, disregarding  $\bar{K}$  condensation



T. Hyodo, W. Weise, arXiv:0712.1613

Critique of phenomenological  $K^-$  potential phen: T. Yamazaki, Y. Akaishi, PRC 76 (2007) 045201 Quasibound  $\bar{K}N$  state: at 1405 MeV (phen) or at 1420 MeV (chiral)?



T. Hyodo, W. Weise, arXiv:0712.1613  $\Lambda(1405)$  shape in  $\pi - \Sigma$  spectrum, calculated in chiral models Do chiral models work well?



N. Barnea, E. Friedman, Phys. Rev. C 75 (2007) 022202 Example of  $K^-$ -Ni (real) potentials in different atomic data fits  $\chi^2$  with respect to 65 data points across the periodic table  $K^-$  atom review: E. Friedman, A. Gal, Phys. Rep. 452 (2007) 89



E. Friedman, A. Gal, Phys. Rep. 452 (2007) 89Deep potential (F) favored over shallow chiral potential



N. Barnea, E. Friedman, Phys. Rev. C 75 (2007) 022202 Functional Derivative analysis  $[\eta = (r - R)/a]$ Deep potential (F) is determined inside the nucleus

**RMF for nucleons and**  $\overline{K}$  mesons  $\mathcal{L}_{K} = (\mathcal{D}_{\mu}K)^{\dagger} (\mathcal{D}^{\mu}K) - m_{K}^{2}K^{\dagger}K + g_{\sigma K}m_{K}K^{\dagger}K \sigma$ 

$$\mathcal{D}_{\mu} \equiv \partial_{\mu} + \mathrm{i} \, g_{\omega K} \, \omega_{\mu} + \mathrm{i} \, g_{\rho K} \, \vec{\tau} \cdot \vec{\rho}_{\mu} + \mathrm{i} \, g_{\phi K} \, \phi_{\mu} + \mathrm{i} \, e \, \frac{1}{2} (1 + \tau_3) A_{\mu}$$

$$\left(-\nabla^2 - E_{K^-}^2 + m_K^2 + \Pi_{K^-}\right)K^- = 0$$

$$\operatorname{Re} \Pi_{K^{-}} = -g_{\sigma K} m_{K} \sigma_{0} - 2E_{K^{-}} (g_{\omega K} \omega_{0} + g_{\rho K} \rho_{0} + g_{\phi K} \phi_{0} + eA_{0}) - (\cdots)^{2}$$

Im  $\Pi_{K^-}$  from  $K^-$  atom fit, considering decay phase space

$$(-\nabla^2 + m_{\sigma}^2)\sigma_0 = +g_{\sigma N}\rho_s + g_2\sigma_0^2 - g_3\sigma_0^3 + g_{\sigma K}m_K K^- K^+$$

$$(-\nabla^2 + m_{\omega}^2)\omega_0 = +g_{\omega N}\rho_v - g_{\omega K}\rho_{K^-}$$

$$(-\nabla^2 + m_{\rho}^2)\rho_0 = +g_{\rho N}\rho_3 - g_{\rho K}\rho_{K^-} \qquad (-\nabla^2 + m_{\phi}^2)\phi_0 = -g_{\phi K}\rho_{K^-}$$

$$2g_{\omega K} = \sqrt{2} g_{\phi K} = 2 g_{\rho K} = g_{\rho \pi} = 6.04$$
 F-type SU(3) (TW)



J. Mareš, E. Friedman, A. Gal, NPA 770 (2006) 84

 $B_{K^-}$  and  $\Gamma_{K^-}$  in RMF calculations: static - empty, dynamical - solid



Average nuclear density  $\overline{\rho}$  for a 1s  $K^-$  bound state



Localized effect of a  $1s K^-$  deeply bound state



D. Gazda, E. Friedman, A. Gal, J. Mareš, PRC 76 (2007) 055204 Dependence on  $(\bar{K}N \to \pi\Sigma) : (\bar{K}NN \to \Sigma N)$ Ratio 0.8 : 0.2 is observed in capture at rest



Conclusion:  $\Gamma_{\bar{K}} > 50$  MeV for deeply bound states



Saturation of  $B_{\bar{K}}$  in <sup>16</sup>O with number of  $\bar{K}$  mesons ( $\kappa$ )



Saturation of <sup>16</sup>O nuclear density with  $\kappa$ , for  $B_{1\bar{K}} = 100 \text{ MeV}$ 



D. Gazda, E. Friedman, A. Gal, J. Mareš, arXiv:0801.3335  $B_{\bar{K}}$  contributions in <sup>16</sup>O: substantial  $\rho$  and  $\phi$  repulsion for  $\bar{K}\bar{K}$  pairs



Saturation of  $B_{\bar{K}}$  in <sup>40</sup>Ca for various RMF nuclear models



Saturation of <sup>40</sup>Ca nuclear density with  $\kappa$ , for  $B_{1\bar{K}} = 100$  MeV



Saturation of  $B_{\bar{K}}$  in <sup>208</sup>Pb with  $\kappa$ , far away from  $\bar{K}$  condensation  $B_{\bar{K}}(\kappa \to \infty) << (m_K + M_N - M_\Lambda) \approx 320 \text{ MeV}$ 



Saturation of  $^{208}\mathrm{Pb}$  nuclear density with  $\kappa,$  for  $B_{1\bar{K}}=100~\mathrm{MeV}$ 



 $1s K^{-}$  effective mass in <sup>208</sup>Pb +  $\kappa K^{-}$ , for  $B_{1\bar{K}} = 100 \text{ MeV}$ 

## Exotic $\overline{K}$ structures, with unbound nuclear cores onset of binding: $K^-pp$ and $\overline{K}^0nn$

Table 1: Binding energies (B) and widths ( $\Gamma$ ) calculated for  $K^-pp$  (in MeV) exclusive of  $\bar{K}NN \to YN$  contributions

	single channel		coupled channels		experiment
	ATMS $[1]$	AMD $[2]$	Faddeev [3]	Faddeev [4]	FINUDA $[5]$
В	48	16-22	50-70	60-95	$115 \pm 6 \pm 4$
Γ	61	40-70	90-110	45-80	$67 \pm 14 \pm 3$

- 1. T. Yamazaki, Y. Akaishi, PLB 535 (2002) 70
- 2. A. Doté, T. Hyodo, W. Weise, NPA (in press) arXiv:0802.0238
- 3. N.V. Shevchenko, A. Gal, J. Mareš, PRL 98 (2007) 082301; PRC 76 (2007) 044004
- 4. Y. Ikeda, T. Sato, PRC **76** (2007) 035203
- 5. M. Agnello et al., PRL 94 (2005) 212303



RMF extension of  $K^-pp$  calculations



Exotic neutrons-only nuclei stabilized by  $\overline{K}^0$  mesons



Saturation of nuclear density in exotic multi- $\bar{K}$  states



Polarization of nuclear cores: neutron single-particle energies



Metastability of exotic neutrons-only multi- $\overline{K}^0$  states

## Summary

- Large widths,  $\Gamma_{\overline{K}} > 50$  MeV, obscure search for single- $\overline{K}$  quasibound nuclear states. Focus searches in light systems
- $\overline{K}$  separation energy saturates in multi- $\overline{K}$  nuclei, and probably also in multi- $\overline{K}$  hypernuclei.  $\overline{K}$  condensation unlikely in self-bound matter on Earth
- $\overline{K}$  condensation in neutron stars is uncertain